

## SYLLABUS

### 1. Data about the program of study

|     |                                |   |
|-----|--------------------------------|---|
| 1.1 | Institution                    | The Technical University of Cluj-Napoca     |
| 1.2 | Faculty                        | Faculty of Automation and Computer Science  |
| 1.3 | Department                     | Computer Science                            |
| 1.4 | Field of study                 | Computer Science and Information Technology |
| 1.5 | Cycle of study                 | Master of Science                           |
| 1.6 | Program of study/Qualification | Data Science                                |
| 1.7 | Form of education              | Full time                                   |
| 1.8 | Subject code                   | 5.00  |

### 2. Data about the subject

|     |                                |   |              |   |                |      |
|-----|--------------------------------|---|--------------|---|----------------|------|
| 2.1 | Subject name                   | Mathematical Models for Machine Learning  |              |   |                |      |
| 2.2 | Subject area                   | Mathematics   |              |   |                |      |
| 2.2 | Course responsible/lecturer    | Prof. Dr Ioan Radu Peter  |              |   |                |      |
| 2.3 | Teachers in charge of seminars | Prof. Dr Ioan Radu Peter  |              |   |                |      |
| 2.4 | Year of study                  | 1   | 2.5 Semester | 1 | 2.6 Assessment | E    |
| 2.7 | Subject category               | Formative category: DA – advanced, DS – speciality, DC – complementary              |              |   |                | DS   |
|     |                                | Optionality: DI – imposed, DO – optional (alternative), DF – optional (free choice) |              |   |                | DFac |

### 3. Estimated total time

|  |                               |    |          |            |     |             |    |               |  |             |  |
|--|-------------------------------|----|----------|------------|-----|-------------|----|---------------|--|-------------|--|
| 3.1  | Number of hours per week      | 2  | of which | 3.2 Course | 1   | 3.3 Seminar | 1  | 3.3 Laborator |  | 3.3 Proiect |  |
| 3.4  | Total hours in the curriculum | 28 | of which | 3.5 Course | 14  | 3.6 Seminar | 14 | 3.6 Laborator |  | 3.6 Proiect |  |
| 3.7 Individual study:  |                               |    |          |            |     |             |    |               |  |             |  |
| (a) Manual, lecture material and notes, bibliography                                 |                               |    |          |            |     |             |    |               |  | 25          |  |
| (b) Supplementary study in the library, online and in the field                      |                               |    |          |            |     |             |    |               |  | 25          |  |
| (c) Preparation for seminars/laboratory works, homework, reports, portfolios, essays |                               |    |          |            |     |             |    |               |  | 20          |  |
| (d) Tutoring   |                               |    |          |            |     |             |    |               |  |             |  |
| (e) Exams and tests  |                               |    |          |            |     |             |    |               |  | 2           |  |
| (f) Other activities   |                               |    |          |            |     |             |    |               |  |             |  |
| 3.8 Total hours of individual study (summ (3.7(a)...3.7(f)))                         |                               |    |          |            | 72  |             |    |               |  |             |  |
| 3.9 Total hours per semester (3.4+3.8)   |                               |    |          |            | 100 |             |    |               |  |             |  |
| 3.10 Number of credit points   |                               |    |          |            | 4   |             |    |               |  |             |  |

### 4. Pre-requisites (where appropriate)

|     |            |                       |
|-----|------------|-----------------------|
| 4.1 | Curriculum | Master of PhD student |
| 4.2 | Competence |                       |

### 5. Requirements (where appropriate)

|     |                      |   |
|-----|----------------------|---|
| 5.1 | For the course       | Computer, projector                         |
| 5.2 | For the applications | 70% presence for entrance to the final exam |

### 6. Specific competences

|     |                          |   |
|-----|--------------------------|---|
| 6.1 | Professional competences | Understanding mathematical models in machine learning, deep learning. |
|-----|--------------------------|---|

|                       |  |
|-----------------------|--|
| 6.2 Cross competences | The ability to apply mathematics for understanding major algorithms, the ability to choose algorithms in problems. |
|-----------------------|--|

**7. Discipline objectives (as results from the *key competences gained*)**

|     |                     |  |
|-----|---------------------|--|
| 7.1 | General objective   | Understanding mathematical models in machine learning, deep learning.  |
| 7.2 | Specific objectives | The ability to apply mathematics for understanding major algorithms, the ability to choose algorithms in problems. |

**8. Contents**

| 8.1. Lecture (syllabus)   | Number of hours | Teaching methods | Notes |
|---|-----------------|------------------|-------|
| Introduction.   | 2               |                  |       |
| Norms. Vector normalizations, meaning.  | 2               |                  |       |
| Generalized Inverse I   | 2               |                  |       |
| Generalized Inverse II  | 2               |                  |       |
| Factorizations (QR, LD etc)   | 2               |                  |       |
| Singular Value Decomposition.   | 2               |                  |       |
| Sparse systems.   | 2               |                  |       |
| Eigenvalues, eigenvectors. Gram Matrices.   | 2               |                  |       |
| Rayleigh quotients. Applications in Machine Learning.   | 2               |                  |       |
| Optimization methods related to Machine Learning.   | 2               |                  |       |
| Classical algorithms using matrix optimization. Principal directions, PCA.  | 2               |                  |       |
| Constrained optimization. Karush-Kuhn-Tucker methods.   | 2               |                  |       |
| Final discussion. Approach methods.   | 2               |                  |       |
| Bibliography<br>Papers related to topics, which have online access. Papers in journals, tutorials, Lecture notes. |                 |                  |       |
| 8.2. Seminars /Laboratory/Project   | Number of hours | Teaching methods | Notes |
| Vector normalization. Generalized inverse I.  | 2               |                  |       |
| Generalized inverse II, factorizations.   | 2               |                  |       |
| Eigenvectors, eigenvalues.  | 2               |                  |       |
| Rayleigh quotients. Applications in Machine Learning.   | 4               |                  |       |
| Constrained optimization. Karush-Kuhn-Tucker methods.   | 2               |                  |       |
| Final discussion. Approach methods.   | 2               |                  |       |
| Bibliography<br>Papers in journals, tutorials, Lecture notes.   |                 |                  |       |

**9. Bridging course contents with the expectations of the representatives of the community, professional associations and employers in the field**

|   |
|---|
| Understanding mathematical models in Machine Learning, Deep learning is a cornerstone for efficient design of algorithms. |
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**10. Evaluation**

|               |                          |                         |                    |
|---------------|--------------------------|-------------------------|--------------------|
| Activity type | 10.1 Assessment criteria | 10.2 Assessment methods | 10.3 Weight in the |
|---------------|--------------------------|-------------------------|--------------------|

|  |  |                |             |
|--|--|----------------|-------------|
|  |  |                | final grade |
| 10.4 Course  | Understanding the teoretical notions, their relations with algorithms. | Written exam.  | 75%         |
| 10.5 Seminars  | Understanding "hidden" mathematical models in different algorithms.    | Seminar grade. | 25%         |
| 10.6 Minimum standard of performance                   |  |                |             |
| Ability to model/present topics and working with them. |  |                |             |

| Date of filling in: | Title               | Surname | Name | Signature |
|---------------------|---------------------|---------|------|-----------|
| Course              | Prof. dr. Ioan Radu | Peter   |      |           |
| Applications        | Prof. dr. Ioan Radu | Peter   |      |           |

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|--|---|
| <b>Date of approval in the department</b><br>20.02.2024      | Head of department<br>Prof.dr.ing. Rodica Potolea |
| <b>Date of approval in the Faculty Council</b><br>22.02.2024 | Dean<br>Prof.dr.ing. Mihaela Dinsoreanu           |